

Number of vertices $n = 10$.

Adjacencies of Graph

1. vertex 1 adjacent to 2 5 6
2. vertex 2 adjacent to 1 3 7
3. vertex 3 adjacent to 2 4 8
4. vertex 4 adjacent to 3 5 9
5. vertex 5 adjacent to 1 4 10
6. vertex 6 adjacent to 1 7 10
7. vertex 7 adjacent to 2 6 8
8. vertex 8 adjacent to 3 7 9
9. vertex 9 adjacent to 4 8 10
10. vertex 10 adjacent to 5 6 9

Size of automorphism group of the graph=20

Full group: $|Aut(polytope)| = 10240$

Restricted group: $|Aut(G) \times switch| = 10240$

Number of orbits for the full group : 5

List of orbits of facets for the full group: Total number of orbits = 5 Total number of facets = 742

1. Inequality 1 with incidence 256 and stabilizer of size 1024. Orbit size is 10 nature: edge inequality $e=[4, 9]$

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|-----------|-----------|------------|------------|-----------|------------|
| (1,2) : 0 | (1,5) : 0 | (1,6) : 0 | (2,3) : 0 | (2,7) : 0 | (3,4) : 0 |
| (3,8) : 0 | (4,5) : 0 | (4,9) : 1 | (5,10) : 0 | (6,7) : 0 | (6,10) : 0 |
| (7,8) : 0 | (8,9) : 0 | (9,10) : 0 | | | |

2. Inequality 2 with incidence 256 and stabilizer of size 256. Orbit size is 40 nature: 4-cycle inequality, $C=[1, 5, 10, 6]$ $F=[1, 5]$

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|-----------|------------|------------|------------|-----------|------------|
| (1,2) : 0 | (1,5) : -1 | (1,6) : 1 | (2,3) : 0 | (2,7) : 0 | (3,4) : 0 |
| (3,8) : 0 | (4,5) : 0 | (4,9) : 0 | (5,10) : 1 | (6,7) : 0 | (6,10) : 1 |
| (7,8) : 0 | (8,9) : 0 | (9,10) : 0 | | | |

3. Inequality 3 with incidence 256 and stabilizer of size 512. Orbit size is 20 nature: edge inequality $e=[9, 10]$

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|-----------|-----------|------------|------------|-----------|------------|
| (1,2) : 0 | (1,5) : 0 | (1,6) : 0 | (2,3) : 0 | (2,7) : 0 | (3,4) : 0 |
| (3,8) : 0 | (4,5) : 0 | (4,9) : 0 | (5,10) : 0 | (6,7) : 0 | (6,10) : 0 |
| (7,8) : 0 | (8,9) : 0 | (9,10) : 1 | | | |

4. Inequality 4 with incidence 160 and stabilizer of size 320. Orbit size is 32 nature: 5-cycle inequality, $C=[8, 9, 10, 6, 7]$ $F=[8, 9]$

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|-----------|------------|------------|------------|-----------|------------|
| (1,2) : 0 | (1,5) : 0 | (1,6) : 0 | (2,3) : 0 | (2,7) : 0 | (3,4) : 0 |
| (3,8) : 0 | (4,5) : 0 | (4,9) : 0 | (5,10) : 0 | (6,7) : 1 | (6,10) : 1 |
| (7,8) : 1 | (8,9) : -1 | (9,10) : 1 | | | |

5. Inequality 5 with incidence 56 and stabilizer of size 16. Orbit size is 640 nature: 7-cycle inequality, $C=[1, 2, 7, 8, 9, 4, 5]$ $F=[1, 2]$

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|------------|-----------|------------|------------|-----------|------------|
| (1,2) : -1 | (1,5) : 1 | (1,6) : 0 | (2,3) : 0 | (2,7) : 1 | (3,4) : 0 |
| (3,8) : 0 | (4,5) : 1 | (4,9) : 1 | (5,10) : 0 | (6,7) : 0 | (6,10) : 0 |
| (7,8) : 1 | (8,9) : 1 | (9,10) : 0 | | | |